## Exercise Set 14

MONOPOLY

III. Questions

ALL GRAPHS ARE IN FIG. 1 AT THE END.

1. Select values for the parameters: $\mathbf{a}=\mathbf{3 0}, \mathbf{F}=\mathbf{6 0}$. (Note: a should be less than 150 .)
2. Sketch the demand curve.

Equation: $\mathrm{P}=150-1.5 \mathrm{Q}$
3. Obtain the marginal revenue function. Sketch the MR curve.
$M R=150-3 Q$ (note: twice as steep as demand, and the vertical intercept is the same as that for demand.)
4. The slope of the MR curve is [ half / same as / twice ] the slope of the demand curve.

Twice.
5. Sketch the MC and AC curves.
6. In order to maximize profits, the firm will produce $\qquad$ units of output and sell them at a price of \$
$\qquad$ each. Explain how how you obtained these values. Indicate the optimal point on the graph.

At the optimal output: $\mathrm{MR}=\mathrm{MC}$
$150-3 Q=30+4 Q$
$7 \mathrm{Q}=120$
$Q=17.14$

Obtain the optimal price from the demand curve.

$$
\begin{aligned}
P & =150-1.5 Q \\
& =150-1.5(17.14) \\
& =124.29
\end{aligned}
$$

7. At the optimal point, we conclude that Price is [ greater than / equal to / less than ] Average Cost. Explain.

$$
A C=a+2 Q+F / Q=30+2(17.14)+60 /(17.14)=67.78
$$

Price is greater than Average cost.
Note: Profit per unit $=P-A C=124.29-67.78=56.51$
8. The price charged by the firm is [ above / below / same as] the marginal revenue and [ above / below / same as ] the marginal cost.
$M R=150-3 Q=150-3(17.14)=98.58$. This is less than Price.
$M C=30+4 Q=30+4(17.14)=98.56$. Same as $M R$ (except for rounding error). Also less than Price.
9. The firm's maximum profit is $\$$ $\qquad$ .

$$
\begin{aligned}
& T R=P \times Q=\$ 2130.69 \\
& T C=30(17.14)+2(17.14)^{2}+60=1161.76 \\
& \text { Profit }=T R-T C=968.93 \text { (due to rounding, numbers may not match those on the website.) }
\end{aligned}
$$

10. If the firm's fixed costs fall, the firm [ will raise / will lower / will not change ] its price and it will produce [ more / less / the same ] output. Explain.

No change in output, since $M R=M C$ has not been affected.
No change in price, since output has not been affected.
11. If the firm's marginal costs rise, the firm [ will raise / will lower / will not change ] its price and it will produce [ more / less / the same ] output. Explain. [Hint: How do you interpret an increase in a?]

Output will fall (from MR = MC)
Price will increase, since output has fallen (see demand curve).

Fig. 1


To find optimal output:
Set $M R=M C$. This yields $Q=17.14$.
To find price:
Read off the price from the demand curve. This yields $P=124.29$.
The average cost at the optimal output is 67.78.

